

The London-Paris link

A fibre link for optical frequency transfer between London and Paris



Objectives

- Understand the basics of optical frequency transfer over fibre
- Recognize equipment necessary to operate a link
- Interpret link parameters and performance
- Give examples of applications

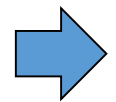
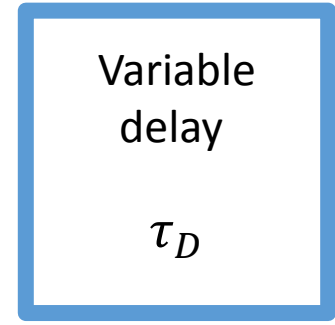
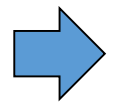
Problem of variable delay noise

Every transmission system has delay:

Transmission system

Stable

phase $\Phi_{in}(t)$
frequency $f_{in} = \frac{d\Phi_{in}}{dt}$



$$\Phi_{out}(t) = \Phi_{in}(t - \tau_D)$$

$$f_{out}(t) = f_{in}(t - \tau_D) \times \left(1 - \frac{d\tau_D}{dt}\right)$$

Unstable / inaccurate 

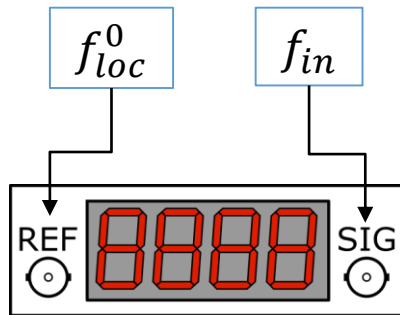
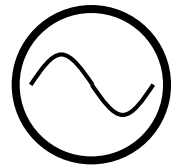
e.g. constant relative velocity
 $\tau_D = (d_0 + vt)/c$ $f_{out} = f_{in} \left(1 - \frac{v}{c}\right)$

Any change of transmission delay causes **“Doppler shift”**.

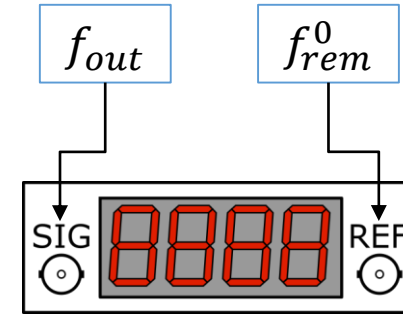
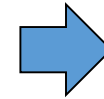
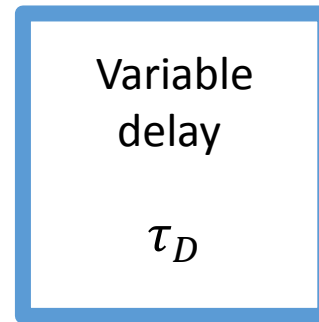
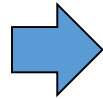
How to measure this noise?

Every frequency measurement needs a reference:

Local
reference

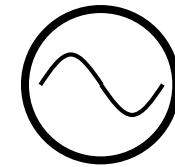


$$\frac{f_{in}}{f_{loc}^0}$$



$$\frac{f_{out}}{f_{rem}^0} = \frac{f_{in}}{f_{loc}^0} \times \frac{f_{loc}^0}{f_{rem}^0} \left(1 - \frac{d\tau_D}{dt} \right)$$

Remote
reference

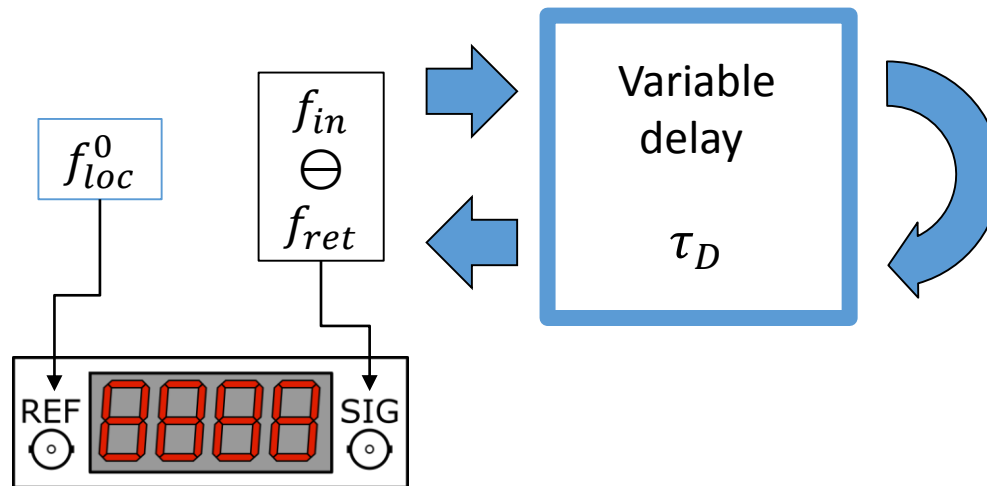


clock mismatch is indistinguishable from Doppler shift.

Principle of delay noise compensation

Solution: double pass transmission

Local reference



$$f_{out} = f_{in} \times \left(1 - \frac{d\tau_D}{dt}\right)$$

Correct

$$\frac{f_{ret} - f_{in}}{f_{loc}^0} = \frac{f_{in}}{f_{loc}^0} \left(1 - 2 \frac{d\tau_D}{dt}\right) \text{ Measure}$$

Measuring the round-trip enables correcting the output

Requires reciprocity!

General principle for time and frequency transfer

e.g. not
10 MHz

e.g. not
GNSS

All non-trivial point-to-point time or frequency transfer methods use the double-pass principle.

Cable or Radio

Fibre or Copper

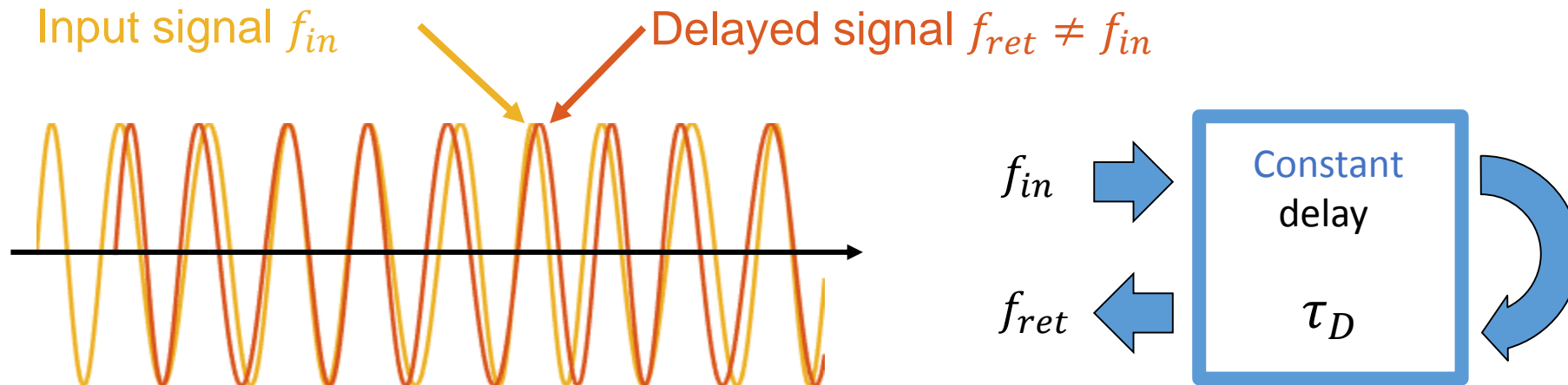
Carrier or Modulated

Packet or Physical layer

Time or Frequency

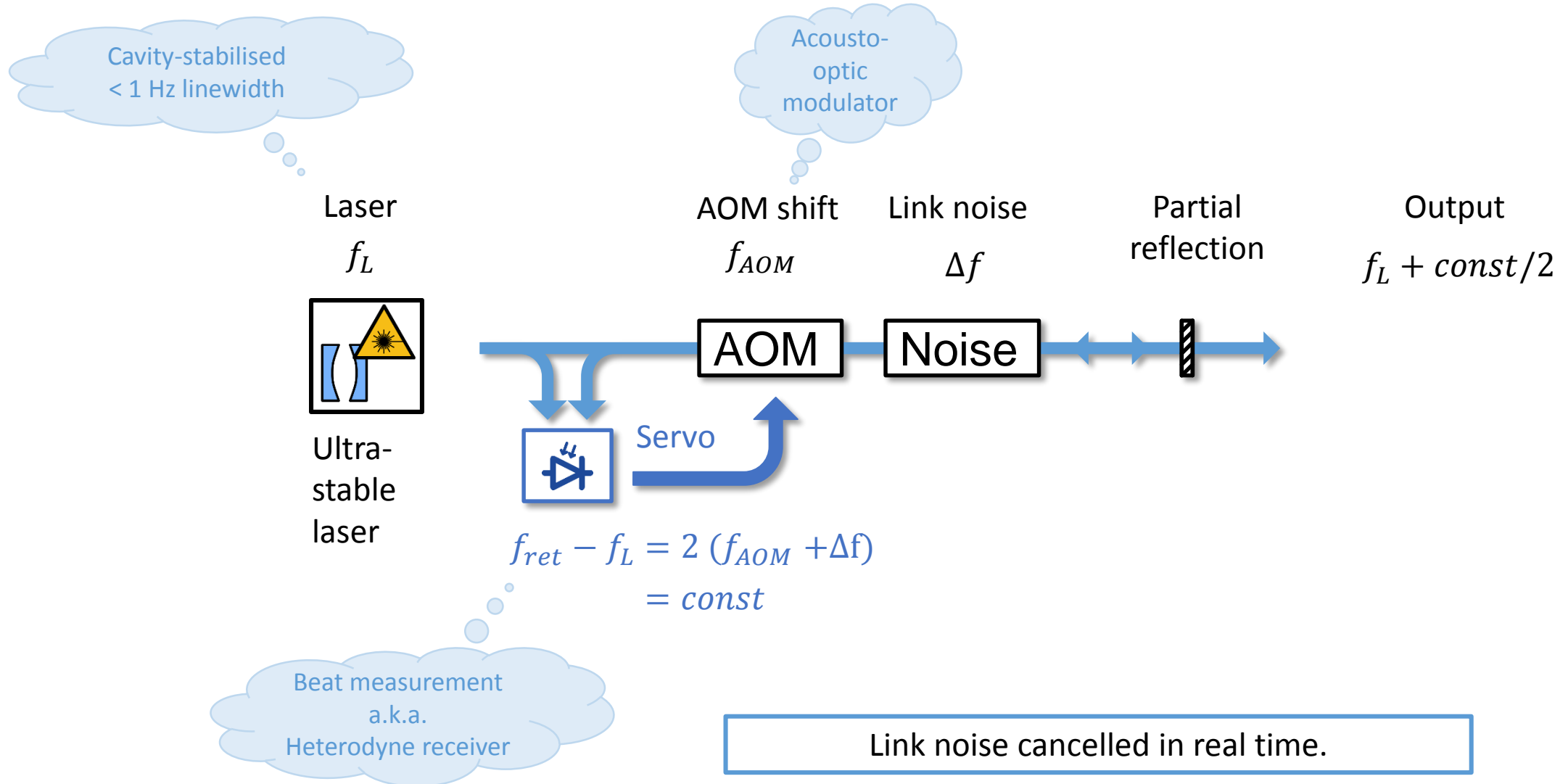
The need for a stable local frequency

Fluctuating input frequency and constant delay:



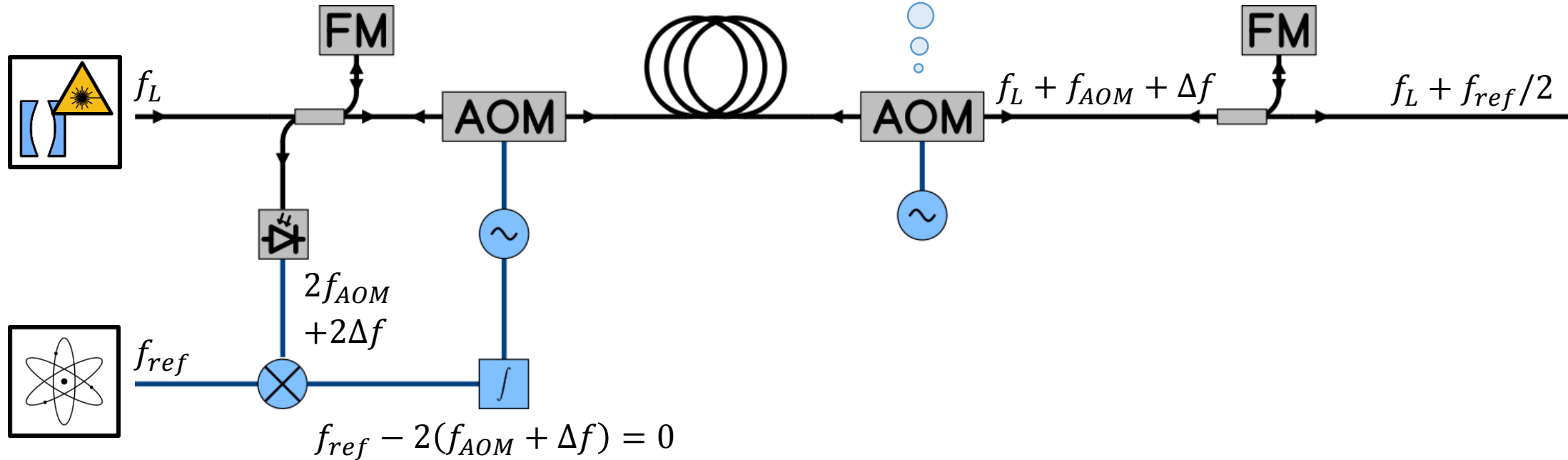
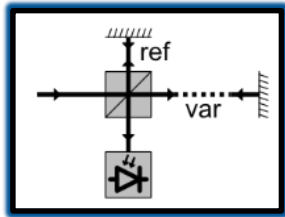
Self-heterodyne noise indistinguishable from delay noise.

Optical frequency transfer over fibre

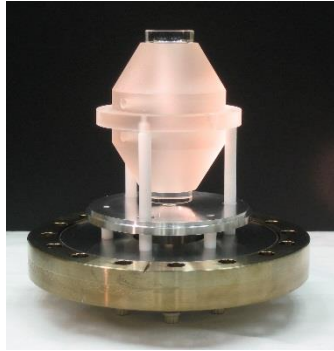


A bit more technical

A very unbalanced Michelson interferometer:



Ultrastable cavity-stabilised laser



Jeff Sherman
CC BY-NC-SA 2.0



NPL

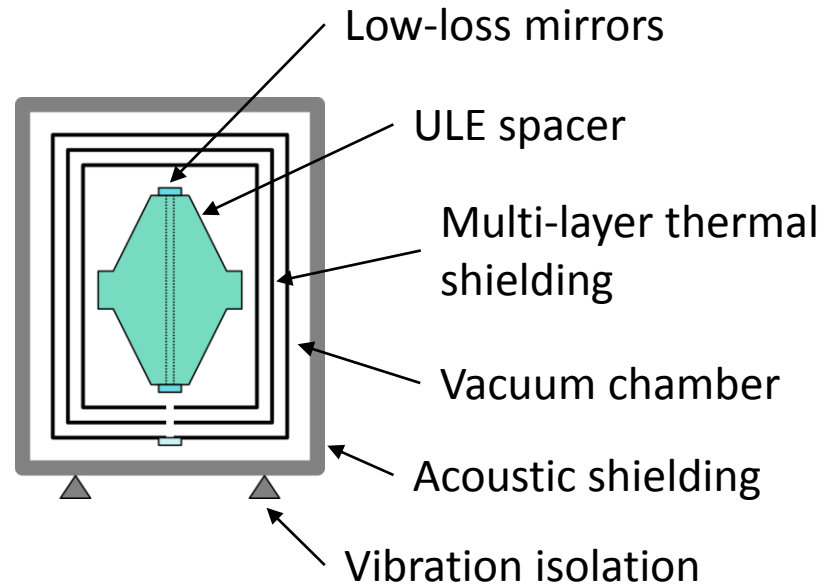
Very high Q resonator



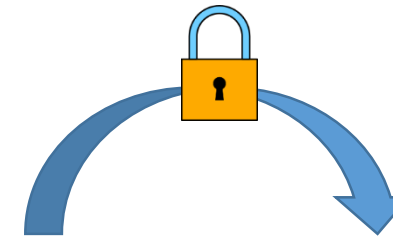
Pound-Drever-Hall



Tunable laser

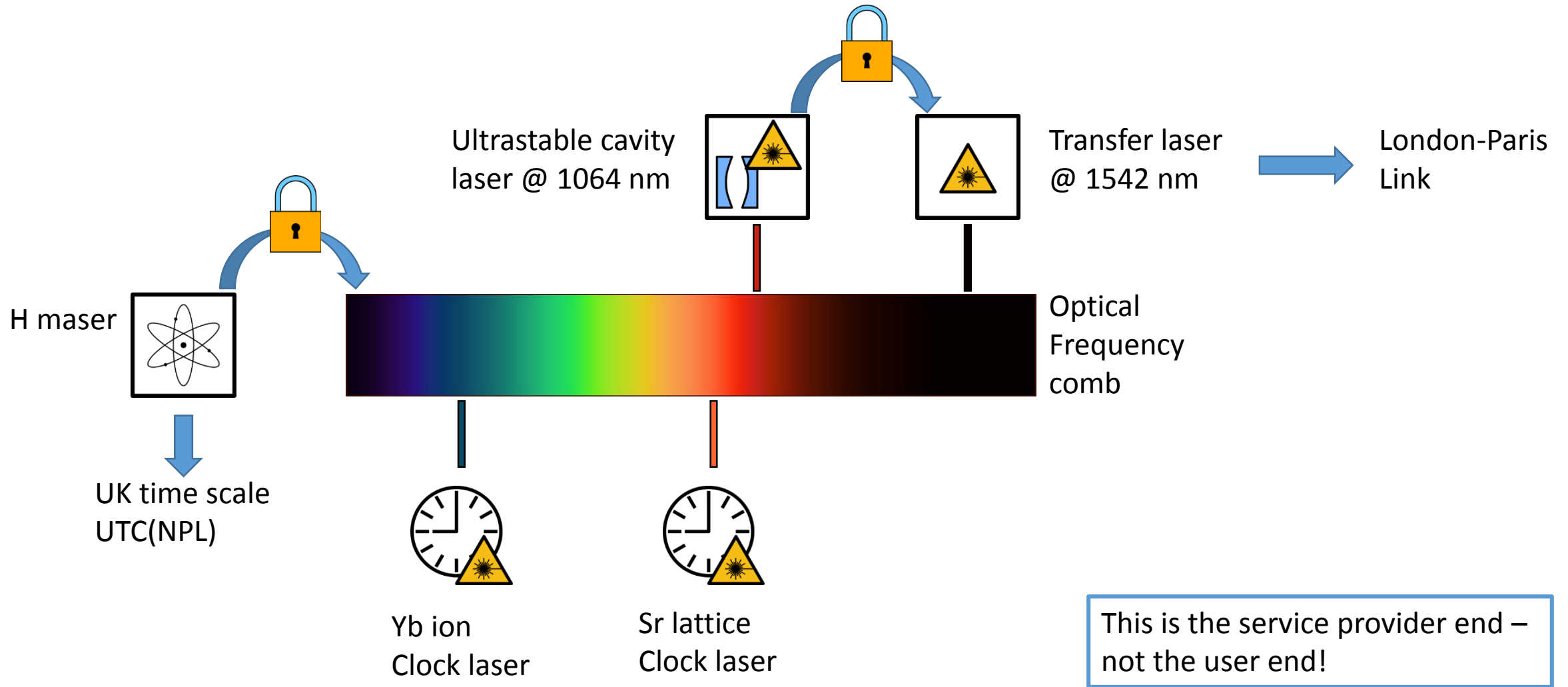


Commercial products available



Sub-Hz linewidth laser

London-Paris link – Local setup



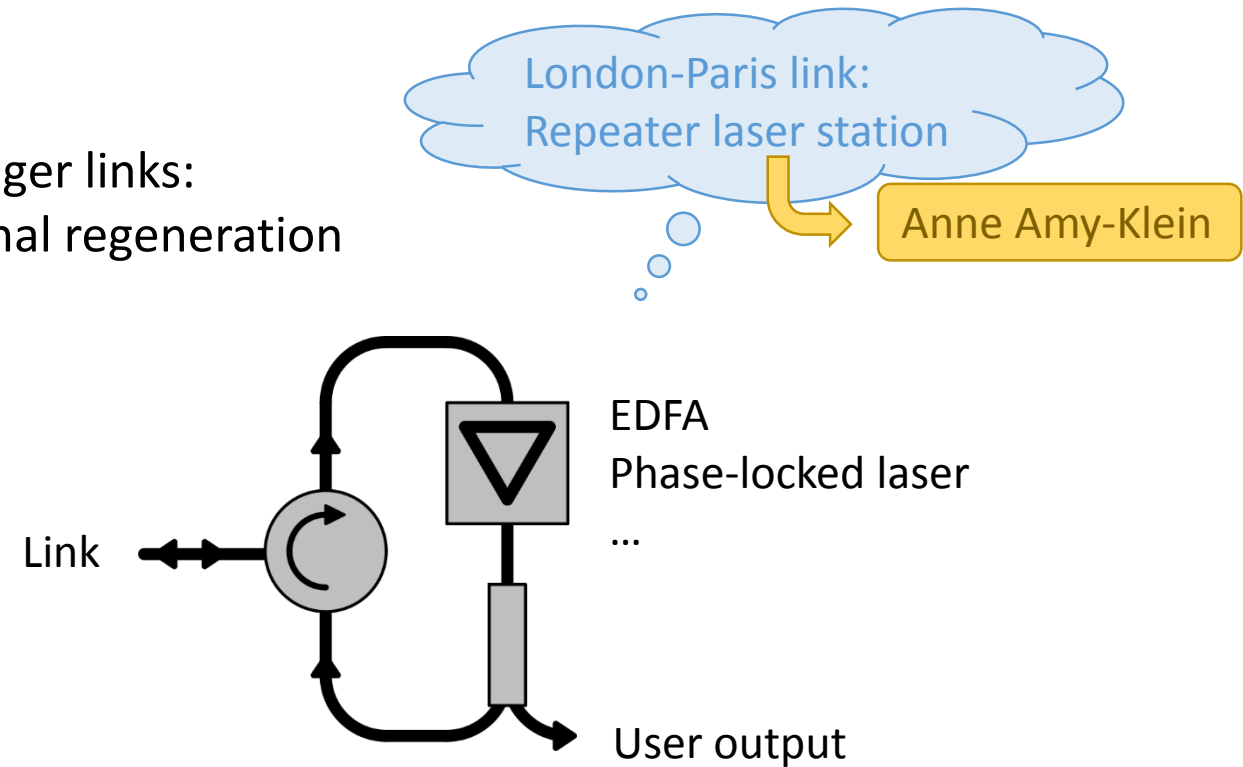
Optical frequency transfer - Remote setup

Simplest case:
Partial Faraday mirror

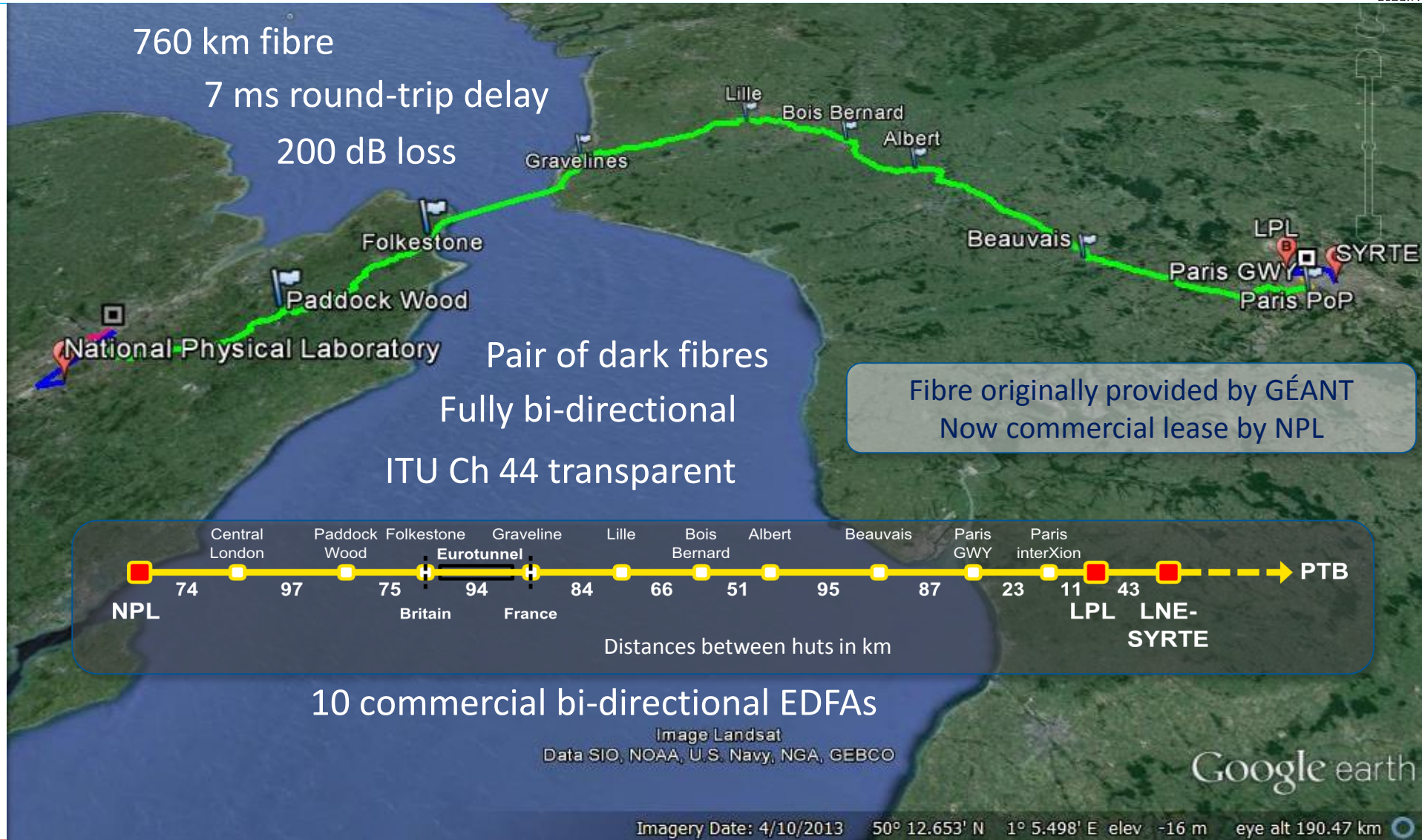


Standard fibre-optic component

Longer links:
Signal regeneration

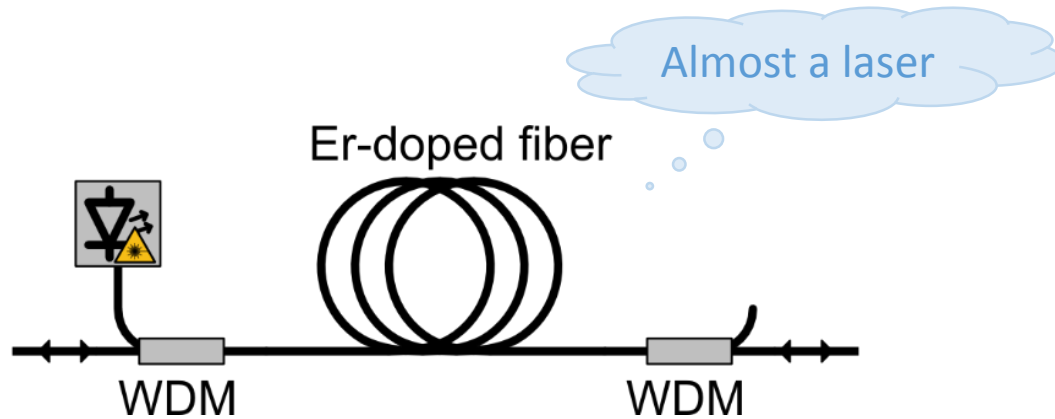


London-Paris link – Fibre route



Amplification techniques

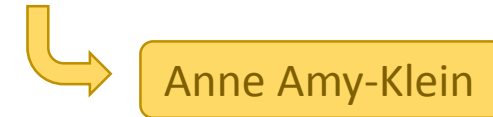
Bidirectional EDFA (Erbium-doped fibre amplifier)



- Gain limited by tendency to oscillate, typically < 15 dB
- Proven technology, benefits from telecom know-how
- Standard telecom EDFAs are **unidirectional, not suitable**

Repeater laser station (RLS)

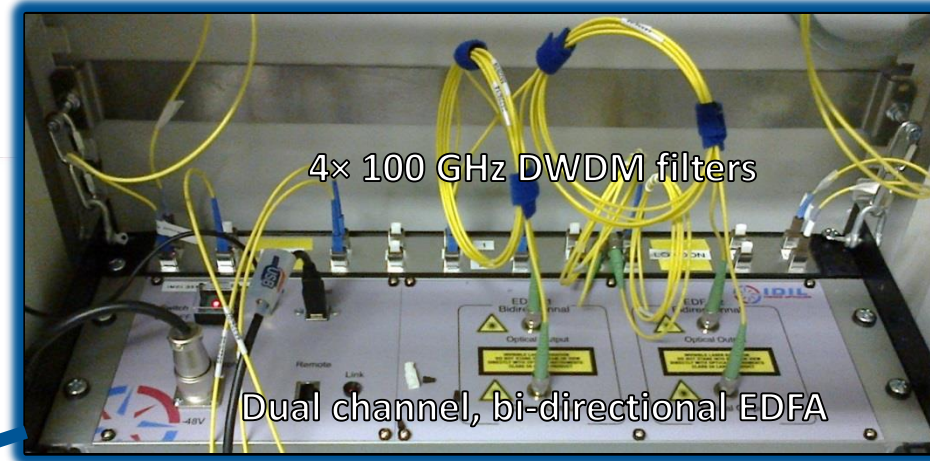
- Essentially a phase locked laser with multiple outputs
- Used to regenerate the signal at the link endpoint



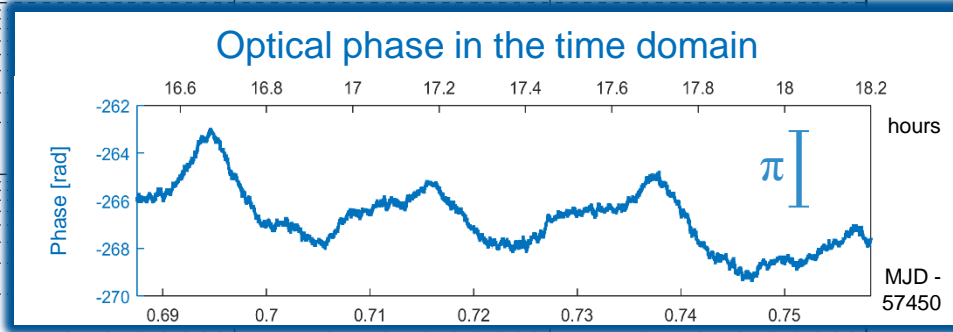
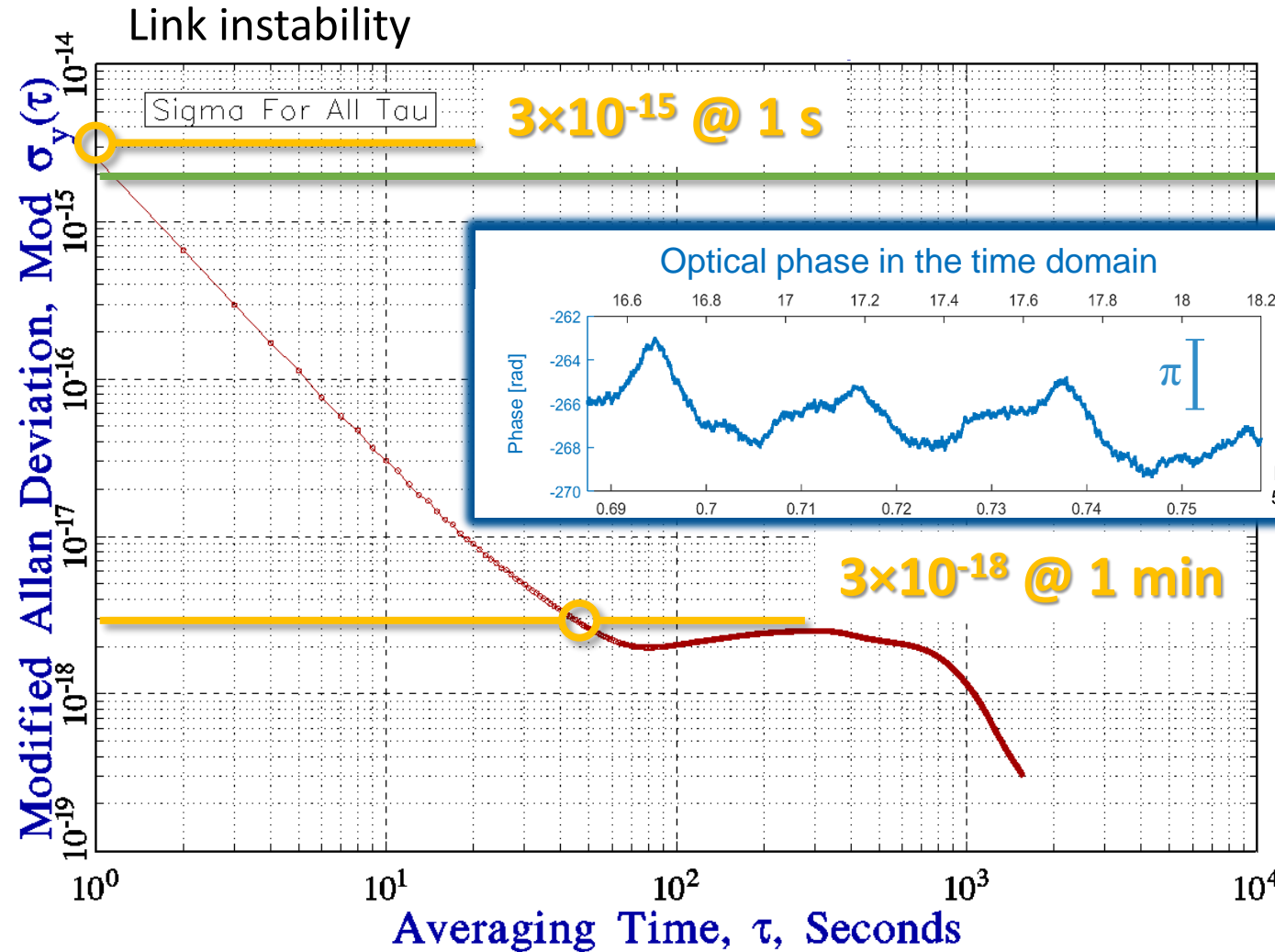
Other options

...

Inside an amplifier hut



Performance



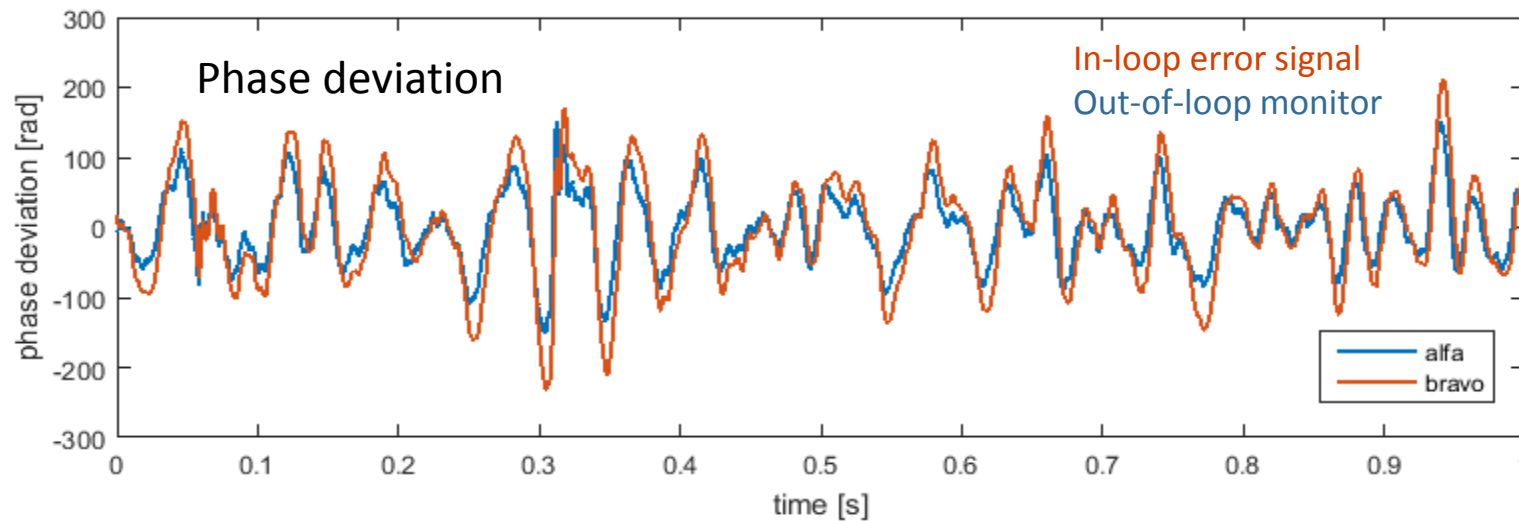
GPS PPP: 2×10^{-15} @ 1 day

J. Leute et al., IEEE TRANSACTIONS ON ULTRASONICS, FERROELECTRICS, AND FREQUENCY CONTROL, p. 981, VOL. 63, NO. 7, JULY 2016

1000× more stable and accurate than GNSS

Limits to performance

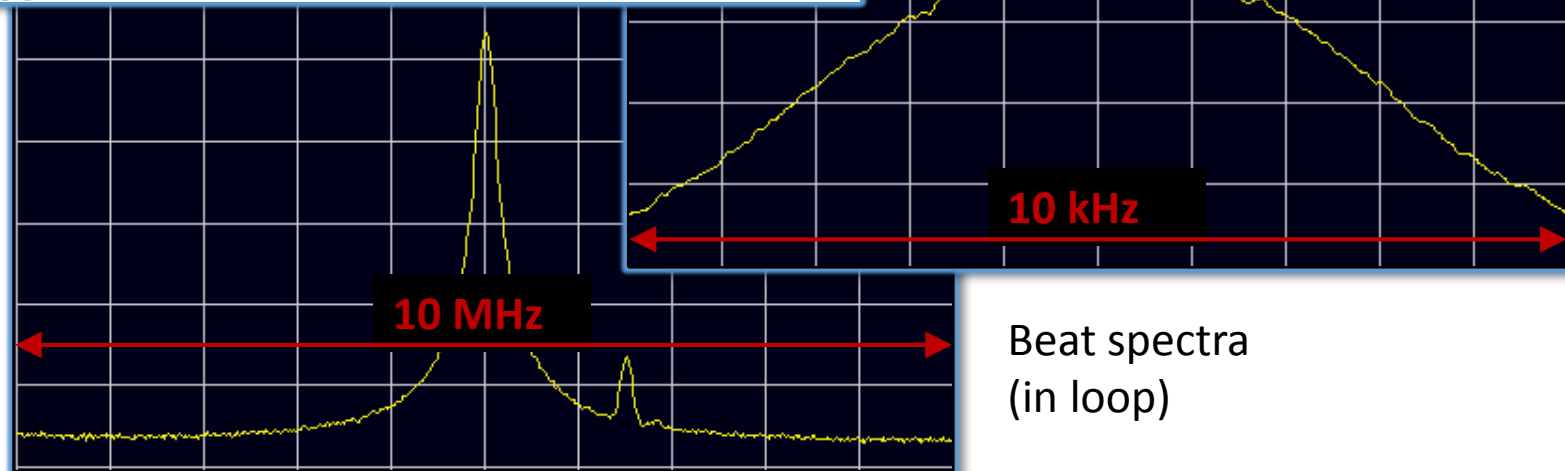
Loop bandwidth limited by round-trip delay



Linewidth $\gg 1$ Hz

Round-trip delay $\tau = 7.3$ ms

Feedback BW $f_{BW} \approx 1/4\tau = 34$ Hz



Applications

➤ Optical clock comparison → Anne Amy-Klein

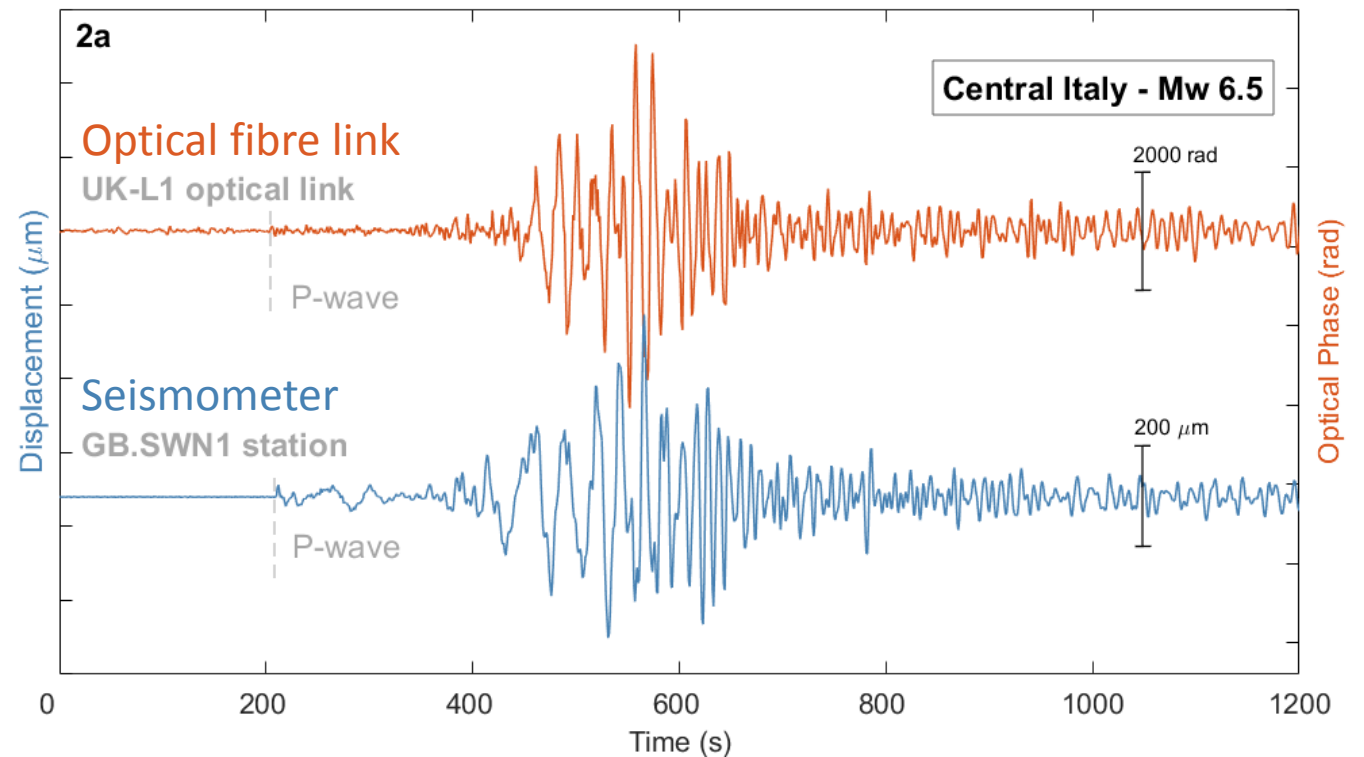
➤ Test of fundamental physics

➤ Earthquake detection

Ultrastable laser interferometry for earthquake detection with terrestrial and submarine cables

GIUSEPPE MARRA, CECILIA CLIVATI, RICHARD LUCKETT, ANNA TAMPELLINI, JOCHEN KRONJÄGER, LOUISE WRIGHT, ALBERTO MURA, FILIPPO LEVI, STEPHEN ROBINSON, ANDRÉ XUEREB, BRIAN BAPTIE, DAVIDE CALONICO

[SCIENCE | 03 AUG 2018 : 486-490](#)



Thank you for your attention



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CLONETS – CLock NETwork Services

Strategy and innovation for clock services over optical-fibre networks

Proposal ID: **731107**

Topic: **INFRAINNOV-2016**

Duration: **30 months**

Start date: **1st January 2017**

Web page: <http://www.clonets.eu>

Coordinator



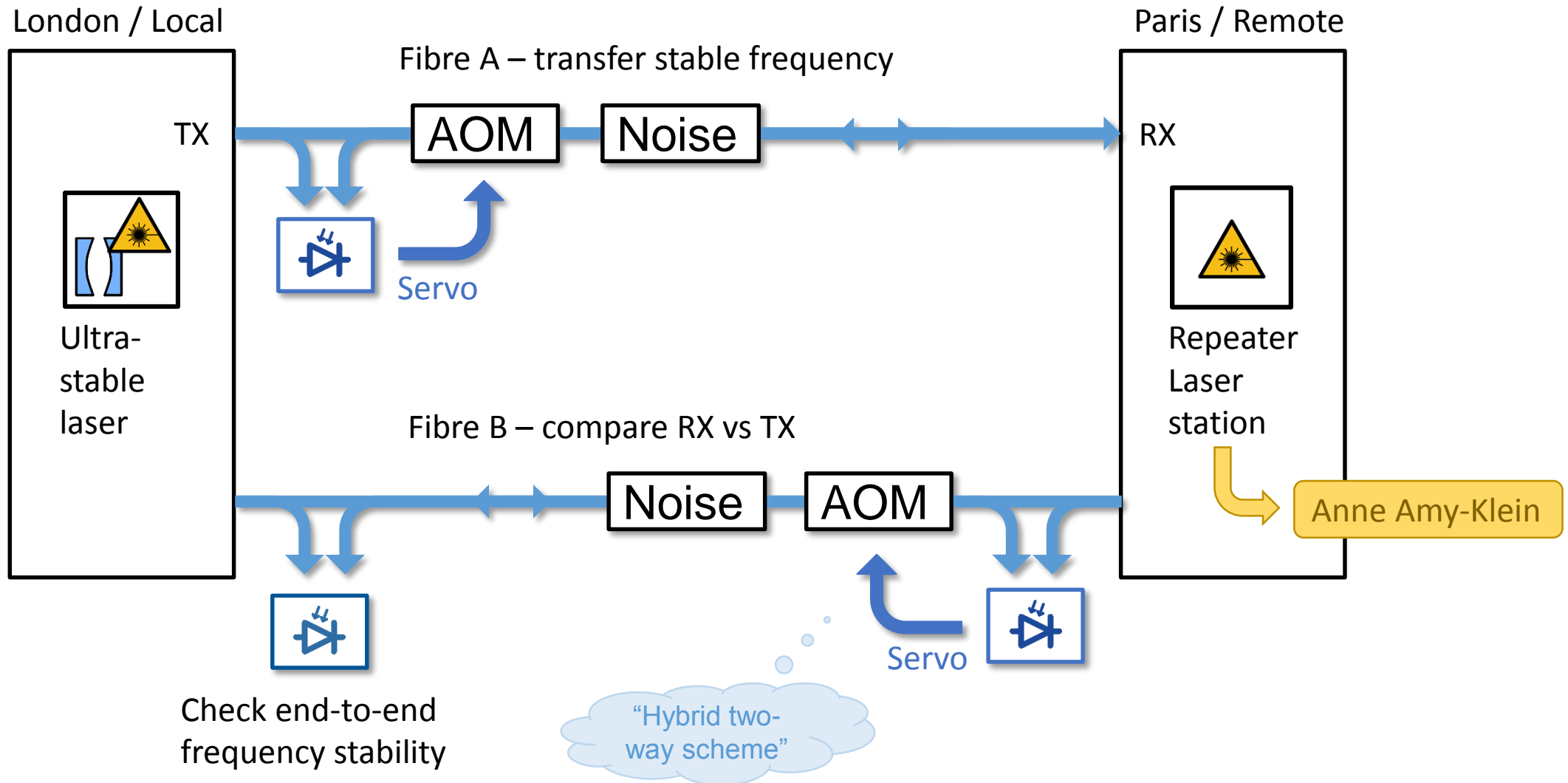
Participants



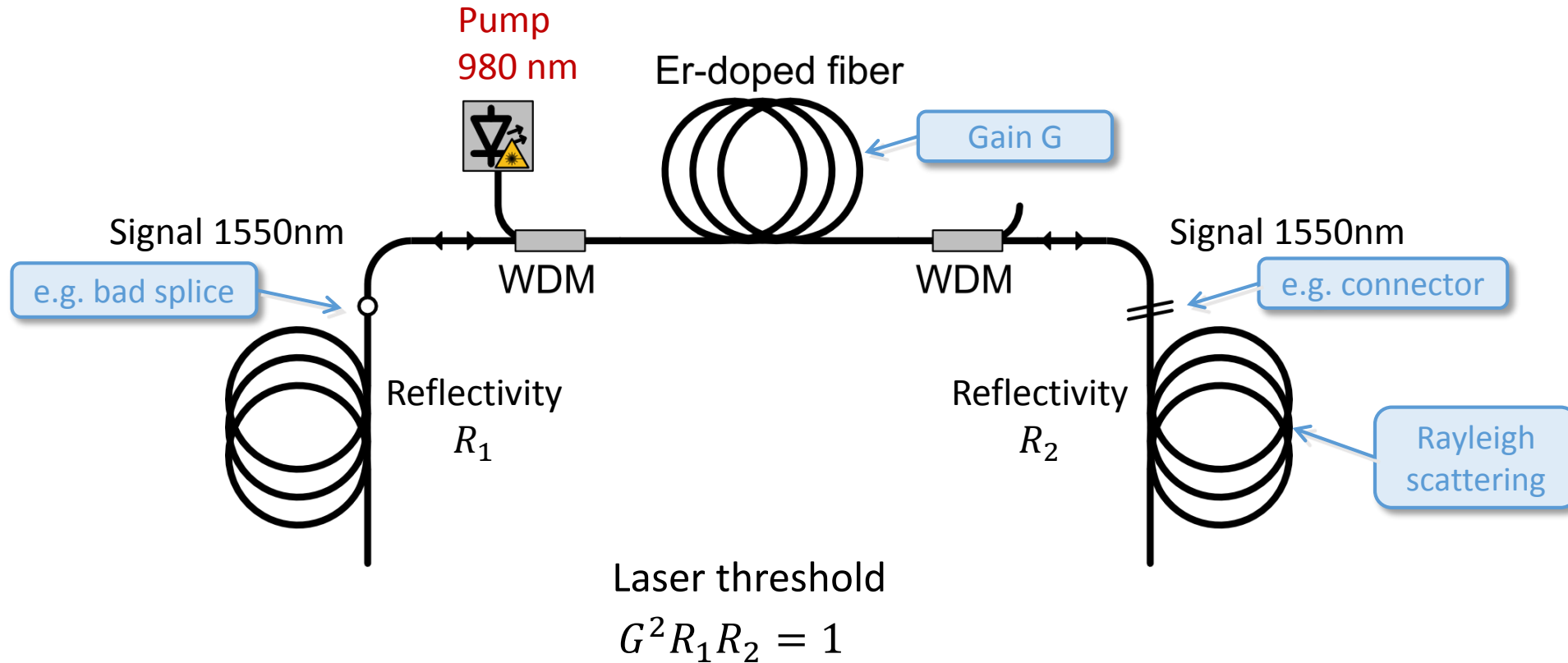
Third Parties



London-Paris link – Topology



Spurious lasing of bidirectional EDFAs



E.g. Rayleigh scattering -35 dB – occasionally much higher
In practice $G = 15...20$ dB max